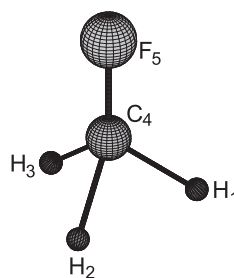


*Fundamentals of Molecular Symmetry*  
 Week 11/11

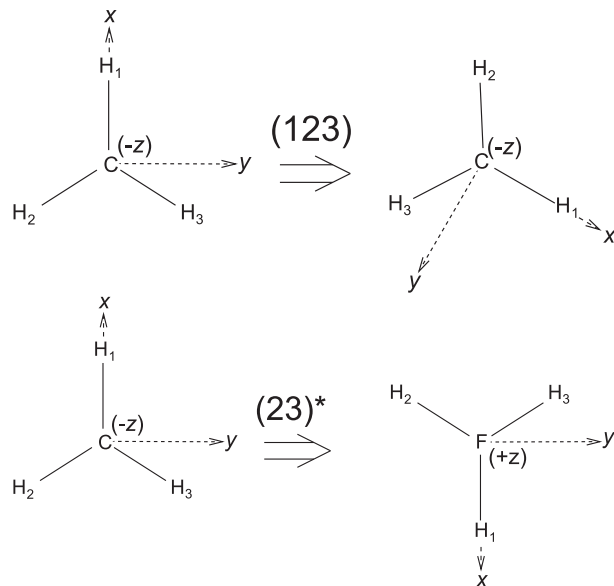
*Exercises*

11.1 We consider the molecule  $\text{CH}_3\text{F}$  discussed in the lecture; the numbering of the nuclei and the character table of the molecular symmetry group  $C_{3v}(\text{M})$  are as follows:



$C_{3v}(\text{M})$ :	$E$	$(123)$	$(23)^*$
	1	2	3
$C_{3v}$ :	$E$	$2C_3$	$3\sigma_v$
Equiv. rot.:	$R^0$	$R_z^{2\pi/3}$	$R_{\pi/2}^{\pi}$
$A_1$ :	1	1	1 : $T_z$
$A_2$ :	1	1	-1 : $R_z, \Gamma^*$
$E$ :	2	-1	0 : $(T_x, T_y), (R_x, R_y)$

The right-handed molecule-fixed axis system  $xyz$  for  $\text{CH}_3\text{F}$  is chosen such that the  $z$  axis lies along the  $\text{CF}$  bond, pointing from  $\text{C}$  towards  $\text{F}$ , and the  $x$  axis lies in the plane defined by the nuclei  $\text{C}$ ,  $\text{F}$ , and proton  $\text{H}_1$ , and pointing from the  $\text{CF}$  axis towards  $\text{H}_1$ . The following two sketches show how the  $xyz$  axis system is affected by the  $(123)$  and  $(23)^*$  operations, respectively. “ $(-z)$ ” indicates that the  $z$  axis points into the plane of the paper; “ $(+z)$ ” that it points out of the paper plane.



- Consider a point in space with coordinates  $(x, y, z)$  in the molecule-fixed axis system. Determine the coordinates  $(x', y', z')$  of this point in the new molecule-fixed axis systems resulting from the application of  $(123)$  and  $(23)^*$ , respectively.
- Use Cartesian displacement coordinates to determine the representation  $\Gamma_Q$  of  $C_{3v}(M)$  (expressed in terms of the irreducible representations) generated by the normal coordinates  $Q_r$  of  $CH_3F$ .
- Determine the representation of  $C_{3v}(M)$  generated by the dipole moment components  $(\mu_x, \mu_y, \mu_z)$  along the molecule-fixed axes for  $CH_3F$ . Determine also the symmetrized linear combinations of  $(\mu_x, \mu_y, \mu_z)$ .